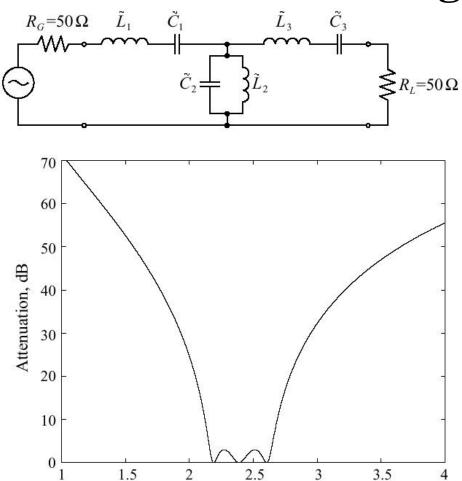
## **Band-Pass Filter Design Example**



Frequency, GHz

Attenuation response of a third-order 3-dB ripple bandpass Chebyshev filter centered at 2.4 GHz. The lower cut-off frequency is  $f_L$  = 2.16 GHz and the upper cut-off frequency is  $f_U$  = 2.64 GHz.

## **RF/mW Stripline Filters**

- Filter components become impractical at frequencies higher than 500 MHz
- Can apply the normalized low pass filter tables for lumped parameter filters to stripline filter design
- Richards Transformation and Kuroda's
   Identities are used to convert lumped
   parameter filter designs to distributed filters

# Richards Transformation: Lumped to Distributed Circuit Design

- Open- and short-circuit transmission line segments emulate inductive and capacitive behavior of discrete components
- Based on:  $Z_{in} = jZ_o tan(\mathbf{b}l) = jZ_o tan(\mathbf{q})$
- Set Electrical Length  $l = \lambda/8$  so

$$\boldsymbol{q} = \boldsymbol{b} \, l = \frac{\boldsymbol{p}}{4} \, \frac{f}{f_o} = \frac{\boldsymbol{p}}{4} \, \Omega$$

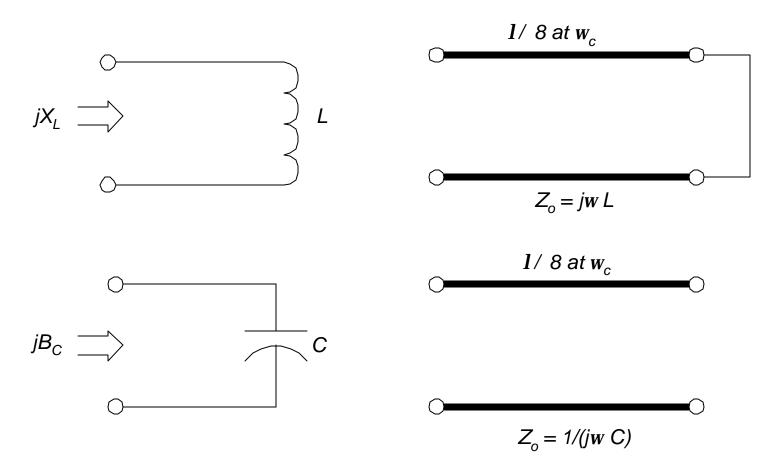
# Richards Transformation: Lumped to Distributed Circuit Design

• Richards Transform is:

$$jX_{L} = j\mathbf{w}L = jZ_{o} \tan\left(\frac{\mathbf{p}}{4}\Omega\right) = SZ_{o}$$
and
$$jB_{C} = j\mathbf{w}C = jY_{o} \tan\left(\frac{\mathbf{p}}{4}\Omega\right) = SY_{o}$$

• For l = 1/8, S = j1 for  $f = f_o = f_c$ 

# Richards Transformation: Lumped to Distributed Circuit Design

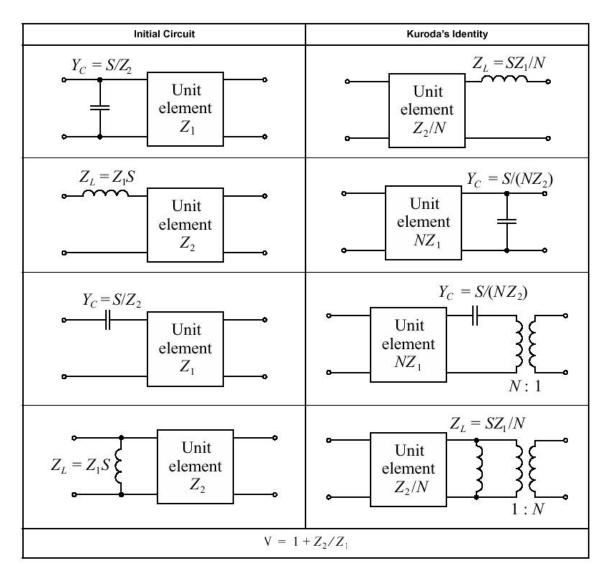


#### **Unit Elements: UE**

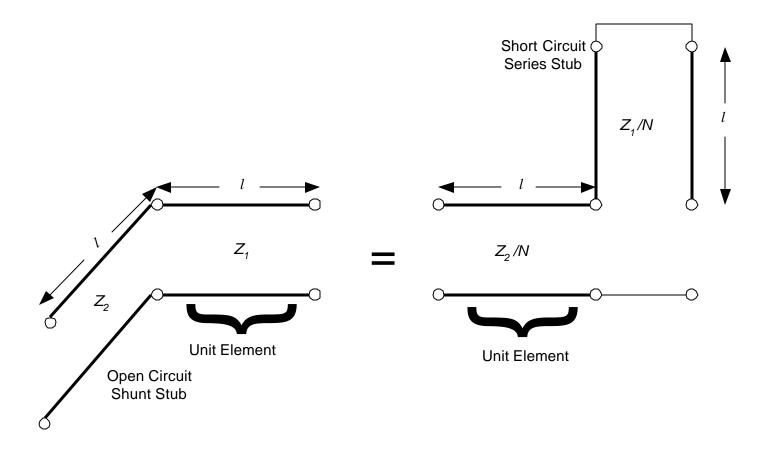
- Separation of transmission line elements achieved by using Unit Elements (UEs)
- UE electrical length: q = pW/4
- UE Characteristic Impedance  $Z_{UE}$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix}_{UE} = \begin{bmatrix} \cos \mathbf{q} & jZ_{UE}\sin \mathbf{q} \\ \frac{j}{Z_{UE}}\sin \mathbf{q} & \cos \mathbf{q} \end{bmatrix} = \frac{1}{\sqrt{1+\Omega^2}} \begin{bmatrix} 1 & j\Omega Z_{UE} \\ \frac{j\Omega}{Z_{UE}} & 1 \end{bmatrix}$$

#### The Four Kuroda's Identities



## Kuroda's Equivalent Circuit



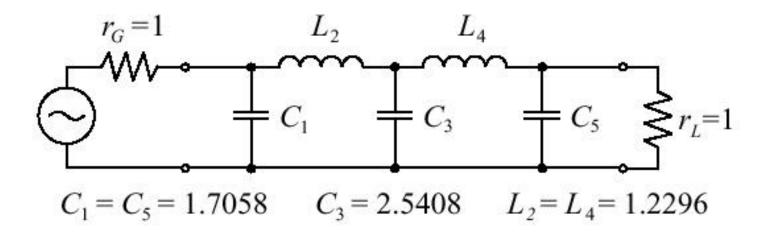
#### Realizations of Distributed Filters

- Kuroda's Identities use redundant transmission line sections to achieve practical microwave filter implementations
- Physically separates line stubs
- Transforms series stubs to shunt stubs or vice versa
- Change practical characteristic impedances into realizable ones

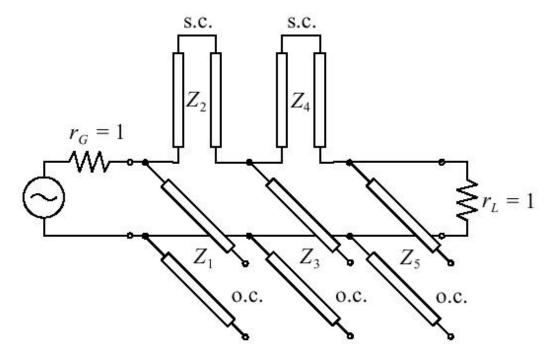
#### Filter Realization Procedure

- Select normalized filter parameters to meet specifications
- Replace L's and C's by  $I_o/8$  transmission lines
- Convert series stubs to shunt stubs using Kuroda's Identities
- Denormalize and select equivalent microstriplines

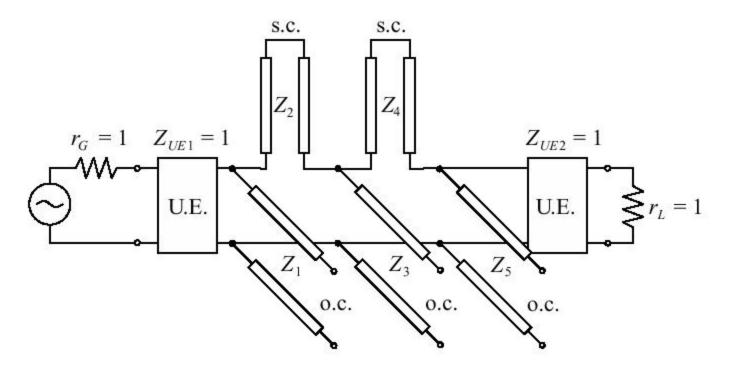
- 5<sup>th</sup> order 0.5 dB ripple Chebyshev LPF
- $g_1 = g_5 = 1.7058$ ,  $g_2 = g_4 = 1.2296$ ,  $g_3 = 2.5408$ ,  $g_6 = 1.0$



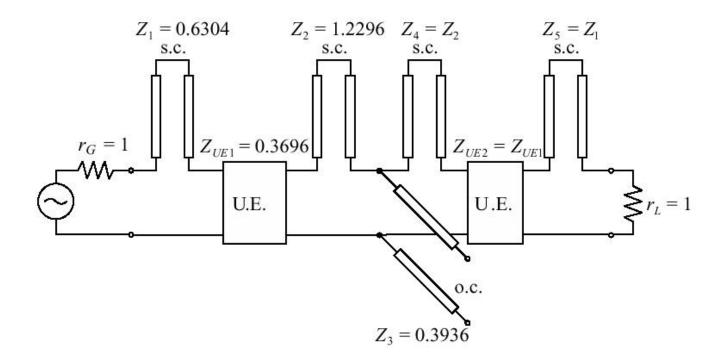
•  $Y_1 = Y_5 = 1.7058$ ,  $Z_2 = Z_4 = 1.2296$ ,  $Y_3 = 2.5408$ ; and  $Z_1 = Z_5 = 1/1.7058$ ,  $Z_3 = 1/2.5408$ 



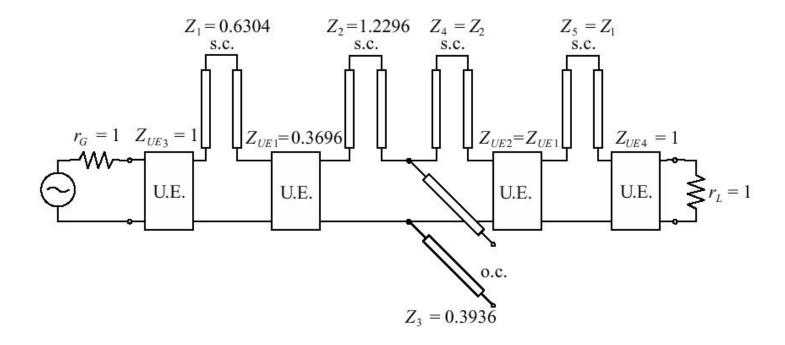
 Utilizing Unit Elements to convert series stubs to shunt stubs



• Apply Kuroda's Identities to eliminate first shunt stub to series stub

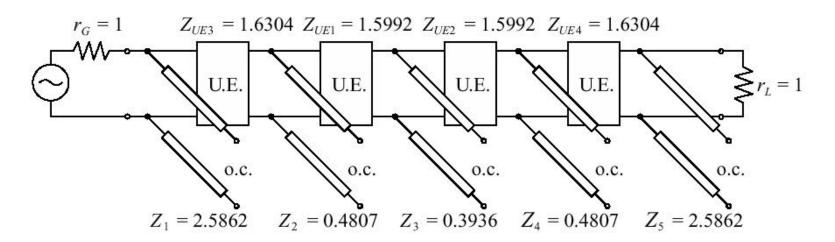


• Deploy second set of UE's in preparation for converting all series stubs to shunt stubs

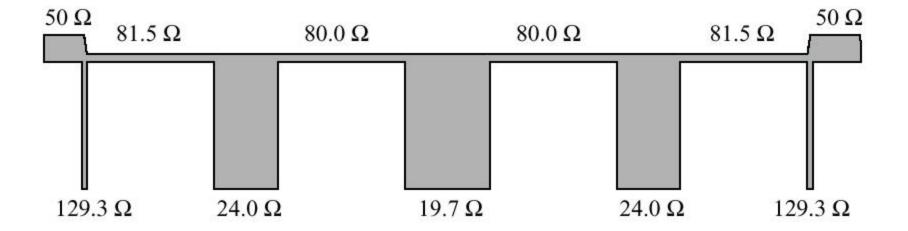


• Apply Kuroda's Identities to eliminate all series stubs to shunt stubs

• 
$$Z_1 = 1/Y_1 = NZ_2 = (1+Z_2/Z_1)Z_2$$
  
=1+(1/0.6304);  $Z_2 = 1$  and  $Z_1 = 0.6304$ 



• Final Implementation



• Frequency Response of the Low Pass Filter

